



**EPFL**

**RESSLab**



# Fire protection engineering

## Exercise - part 1

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# Calculation example

Using the nomogram in accordance with EN 1993-1-2:2005 and the SZS tables, answer the questions below:

- Determine the fire resistance of the various sections subjected to the action of the fire and check whether resistance R 30 is achieved?
- If the strength of the IPE 360 beam is not sufficient, determine the thickness of the plasterboard required to achieve this strength?

# Calculation example

This is a two-storey metal hall with an industrial use and a thermal load  $q < 1,000 \text{ MJ/m}^2$ . The ground floor is used for timber frame production, and the first floor houses the company's offices.

The charges to be taken into consideration are as follows:

## *Roof*

Dead weight of the structure	0.50 kN/m <sup>2</sup>
Dead weight of the sheet	0.20 kN/m <sup>2</sup>
Insulation + waterproofing	0.10 kN/m <sup>2</sup>
Gravel 8-16	1.25 kN/m <sup>2</sup>
Snow (alt. 450 m)	0.90 kN/m <sup>2</sup>

## *Intermediate slab*

Dead weight of the structure	0.50 kN/m <sup>2</sup>
Dead weight of 12 cm slab	3.00 kN/m <sup>2</sup>
Screens	0.50 kN/m <sup>2</sup>
Screed + finish	2.50 kN/m <sup>2</sup>
Payload for administrative premises.	3.00 kN/m <sup>2</sup>

# Calculation example

The static system is described below and the hall is braced in both directions at each frame level, with a frame spacing of 4.00 m. For the columns, take a buckling length  $l_{ky} = l_{kz} = l$ . All columns are exposed to fire on all 4 sides.

The load descent must be carried out with all surfaces loaded (no checkerboard loading), checking only the normal forces (pillars) and bending forces (beam).

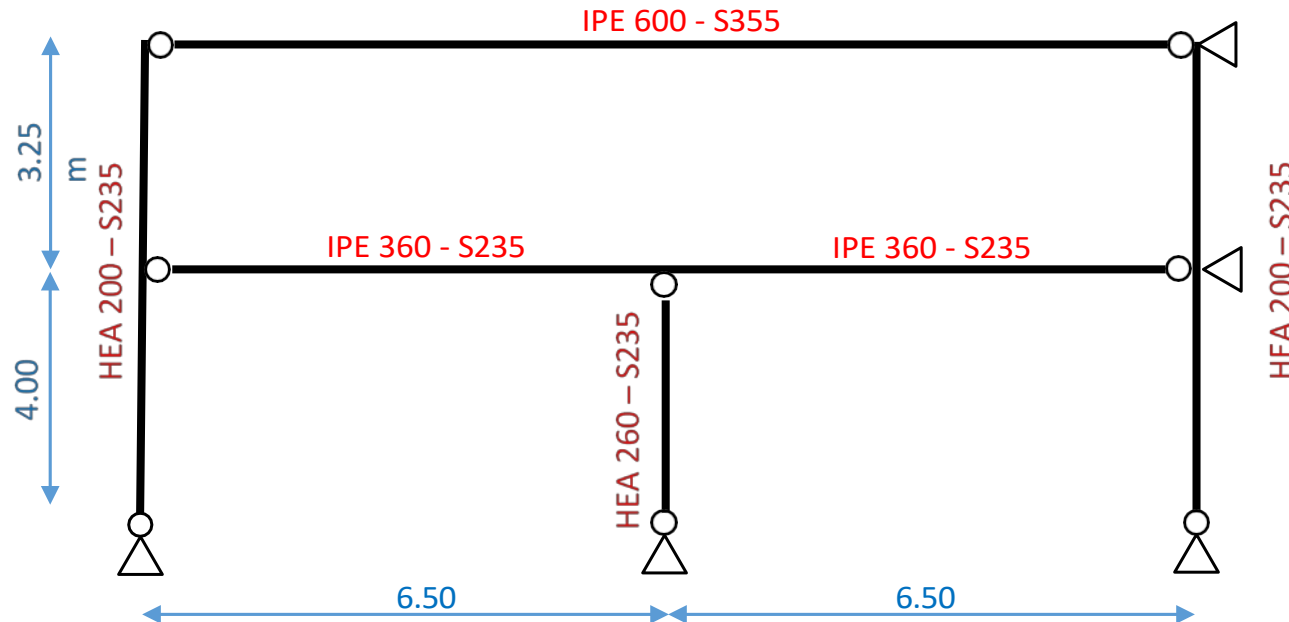


Table 1

Height category	Low-rise buildings (up to a total height of 11 m)				
Allocation	Concept	Support system [1]	Floor slabs fOFM fire compartments	Forced walls ments, firebreaks and horizontal evacuation routes	Vertical drainage-ways
<ul style="list-style-type: none"> <li>Residential buildings housing several dwellings</li> <li>Offices</li> <li>Schools</li> <li>Sales premises (with a fire compartment surface area of up to 1'200 m* and accommodating up to 300 people)</li> <li>Car parks [3]</li> <li>Industry and craft q up to 1'000 MJ/m²</li> <li>Agriculture</li> </ul>	Construction	R 30	REI 30 [s]	EI 30	REI 30
	Extinguishing system	no exigency	EI 30	EI 30	REI 30
<ul style="list-style-type: none"> <li>Industry and crafts q greater than 1,000 MJ/m</li> </ul>	Construction	R 60	REI 00 [5]	EI 60 [2] [5]	REI 60
	Installation extinction	R 30	REI 30 [5]	EI 30	REI 60
<ul style="list-style-type: none"> <li>Residential facilities [a] e.g. retirement and nursing homes</li> </ul>	Construction	R60	REI 60	LI60	REI 60
	Installation extinction	R30	REI 30	EI 30	REI 60
<ul style="list-style-type: none"> <li>Accommodation establishments [b] e.g. hotels</li> <li>Isolated accommodation establishments [c][5] e.g. mountain refuges</li> <li>Premises receiving a large number of people</li> <li>Department stores</li> </ul>	Construction	R 60	REI d0	9  99	RLI 60
	Extinguishing system	R 30	REI 30	EI30	REI 60

• no requirements load-bearing construction elements are not subject to any fire resistance requirements

[1] In single-storey buildings, as well as in the top storey of multi-storey buildings, load-bearing construction elements are not subject to any fire resistance requirements.

[2] In single-storey buildings, and on the top storey of multi-storey buildings, the fire resistance of the walls forming the fire compartments may be limited to 30 minutes.

[3] When the perimeter walls contain at least 25% of openings that cannot be closed, no fire resistance requirements are imposed on load-bearing structural elements in category RF1 in areas located no more than 35 m from an opening that cannot be closed.

[4] It is not compulsory to install a fire detection system in accommodation establishments.

1 Versi on as per AIET dec lson of 22 September 2018

## ANNEX A (normative)

### BUILDINGS

Table 2: Reduction coefficients for buildings

Actions	$\psi_0$	$\psi_1$	$\psi_2$
<b>Payloads in buildings</b> – Category A Residential premises Category B Administrative premises – Category C Meeting rooms – Category D Sales premises Category E Warehouses	0,7 0,7 0,7 0,7 1,0	0,5 0,5 0,7 0,7 0,9	0,3 0,3 0,6 0,6 0,8
<b>Traffic loads in buildings</b> – Category F Vehicles under 3.5 t Category G Vehicles from 3.5 t to 16 t – Category H Roofs	0,7 0,7 0	0,7 0,5 0	0,6 0,3 0
Snow loads	$1 - 60/l_0$	$1 - 250/l_j$	$1 - 1000/l_l$
Wind forces	0,6	0,5	0
Effects of temperature	0,6	0,5	0
<b>Foundation actions</b> – Land thrust – Hydraulic pressure	0,7 0,7	0,7 0,7	0,7 0,7

Table 3: Indicative values for floor and beam deflections

Limit state	Consequences of the effects of actions		
	irreversible	reversible	reversible
		Load cases	
	rare (20)	common (21)	quasi-permanent (22)
<b>Ability to operate</b> – Fragile built-in elements – Incorporated ductile elements Use and operation	$w \leq l/500$ <sup>1) 2)</sup>	$w \leq l/350$ <sup>1)</sup> $s \leq l/350$ <sup>!3)</sup>	
Comfort		$w' \leq l/350$ <sup>!3)</sup>	
Aspect			$w \leq l/300$ <sup>!4)</sup>
<sup>1*</sup> Deflection due to actions, particularly long-term actions, after all the secondary construction elements have been fitted and the technical equipment installed. <sup>2!</sup> If built-in elements react particularly sensitively to deformations in the supporting structure, constructive measures against damage must be taken first and foremost, in addition to or instead of the measures resulting from the dimensioning procedure. <sup>3!</sup> Deflection due solely to variable actions. <sup>!4*</sup> Arrow, after deduction of any counter-arrow. Any long-term effects must be taken into account.			
Deflections will be determined in accordance with SIA standards 262 to 266.  Different limit values for the booms may be agreed in accordance with the requirements of use. These will be recorded in the design basis. Reduced requirements are possible especially for secondary construction elements.			

Querschnittswiderstände (Bemessungswerte) Section resistances (values of calculation)

$$N_{Rd} = f_y \cdot A / \gamma_{M1} \quad (1)$$

$$V_{Rd} = \tau_y \cdot A_v / \gamma_{M1} \quad (1)$$

$$M_{y,Rd} = f_y \cdot W_{ply} / \gamma_{M1} \quad (1)$$

$$M_{z,Rd} = f_y \cdot W_{plz} / \gamma_{M1} \quad (1)$$

$$d \frac{A - 2btt}{A} \dot{A} \frac{1}{1-a/2}$$

$$c_s = \frac{(t + 2k)^{-1}}{A_w}$$

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 Interaktion siehe Norm SIA 263 Cumulation prohibited  
 Interaction see SIA 263

a, f: Hilfswerte für die Formeln (44-48) der Norm SIA 263: 2013.  
 CS: Hilfswert für Stützenprofile in Rahmen knoten gemäss ersetzter Norm SIA 263: 2003, Ziffer 6.6.3.3.

a, \dot{A}: Auxiliary values for formulas f44-48j of standard SIA 263: 20/3.

aS: Auxiliary value for column sections in frame nodes in accordance with the superseded standard SIA 263: 2003, section 6.6.3.3.

° siehe S. 26+34 / see p. 26+34

CAI	m	ly 10 <sup>4</sup>	Hilfswerte Auxiliary values a t as mm				S235				Verfahren Méthode PP EP		S355				Verfahren Méthode PP EP	
							Querschnittswiderstände Re "ist nces of sections						Querschnittswiderstände Section continuity 0					
							NRd	VRd	My Rd	M <sup>o</sup> Rd	NRd	VRd	My Rd	M <sup>o</sup> Rd	NRd	VRd	My Rd	M <sup>o</sup> Rd
kN	kN	kNm	kNm	kN	kN	kNm	kNm	kN	kN	kNm	kNm							
80*	6,0	0,80	0,37	1,23	26	171	46	5,20	1,30	1,0	1,0	258	70	7,85	1,97	1,0	1,0	
100*	8,1	1,71	0,39	1,24	33	231	66	8,82	2,05	1,0	1,0	349	99	13,3	3,09	1,0	1,0	
120*	10,4	3,18	0,39	1,24	33	296	81	13,6	3,04	1,0	1,0	447	123	20,5	4,59	1,0	1,0	
140*	12,9	5,41	0,39	1,24	34	368	99	19,8	4,31	1,0	1,0	555	149	29,9	6,51	1,0	1,0	
160*	15,8	8,69	0,40	1,25	41	450	125	27,7	5,84	1,0	1,0	679	189	41,9	8,82	1,0	1,0	
180*	18,8	13,2	0,39	1,24	42	536	145	37,2	7,74	1,0	1,0	810	220	56,3	11,7	0,31	1,0	
200*	22,4	19,4	0,40	1,25	54	638	181	49,4	10,0	1,0	1,0	963	273	74,6	15,1	0,28	1,0	
220*	26,4	27,7	0,39	1,24	56	747	205	63,9	13,0	1,0	1,0	1128	310	96,5	19,6	0,25	1,0	
240*	30,7	38,9	0,40	1,25	69	875	247	82,1	16,5	1,0	1,0	1323	374	124,0	25,0	0,23	1,0	
270*	36,1	57,9	0,40	1,25	68	1028	286	108,3	21,7	0,31	1,0	1553	432	163,6	32,8	0,20	0,27	
300*	42,2	83,6	0,40	1,25	66	1204	332	140,6	28,0	0,29	1,0	1819	501	212,4	42,3	0,19	0,26	
330*	49,1	117,7	0,41	1,26	77	1401	398	180,0	34,4	0,27	1,0	2117	601	271,9	52,0	0,17	0,24	
360*	57,1	162,7	0,41	1,25	79	1628	454	228,1	42,8	0,26	1,0	2459	686	344,6	64,6	0,16	0,22	
400*	66,3	231,3	0,42	1,27	86	1890	552	292,6	51,3	0,25	0,33	2856	833	441,9	77,4	0,15	0,21	
450*	77,6	337,4	0,44	1,28	80	2212	657	380,9	61,9	0,24	0,32	3341	992	575,4	93,4	0,14	0,21	
500*	90,7	482,0	0,45	1,29	78	2585	774	491,1	75,2	0,23	0,31	3906	1169	741,8	113,6	0,13	0,20	
550	106	671,2	0,46	1,30	83	3008	935	623,8	89,6	0,23	0,32	4545	1412	942,3	135,4	0,13	0,20	
600	122	920,8	0,46	1,30	83	3491	1083	786,1	108,7	0,23	0,31	5274	1635	1188	164,2	0,12	0,19	
750x137	1599		0,49	1,32	54	3907	1200	1089	137,4	0,08	0,15	5903	1813	1645	207,6	N	0,05	
750x147	1661		0,50	1,33	47	4196	1362	1144	141,2	0,16	0,24	6339	2058	1728	213,3	0,05	0,12	
750x173	2058		0,48	1,31	60	4954	1505	1392	181,3	0,19	0,28	7483	2273	2102	273,8	0,09	0,16	
750x196	2403		0,46	1,30	69	5614	1645	1606	214,6	0,23	0,32	8480	2484	2426	324,2	0,12	0,19	
<b>HEA</b>																		
100*	16,7	3,49	0,25	1,14	122	475	98	18,6	9,21	1,0	1,0	718	147	28,1	13,9	1,0	1,0	
120*	19,9	6,06	0,24	1,14	121	567	109	26,7	13,2	1,0	1,0	857	165	40,4	19,9	1,0	1,0	
140*	24,7	10,3	0,24	1,14	117	703	131	38,8	19,0	1,0	1,0	1062	198	58,7	28,7	1,0	1,0	
160*	30,4	16,7	0,26	1,15	137	868	171	54,9	26,3	1,0	1,0	1311	258	82,9	39,8	1,0	1,0	
180*	35,5	25,1	0,24	1,14	145	1013	187	72,2	35,0	1,0	1,0	1530	282	109,8	52,9	N	1,0	
200*	42,3	36,9	0,26	1,15	166	1205	234	96,1	45,6	1,0	1,0	1820	353	145,2	68,9	N	1,0	
220*	50,5	54,1	0,25	1,14	170	1440	267	127,2	60,6	1,0	1,0	2175	404	192,2	91,5	N	1,0	
240*	60,3	77,6	0,25	1,14	200	1720	325	166,7	78,7	1,0	1,0	2598	491	251,8	118,9	N	1,0	
260*	68,2	104,5	0,25	1,14	234	1943	372	205,9	96,3	1,0	1,0	2935	561	297,9 <sup>^</sup>	95,3 <sup>^</sup>	N	N	
280*	76,4	136,7	0,25	1,14	228	2177	410	248,9	116,0	1,0	1,0	3288	620	358,4 <sup>^</sup>	115,0 <sup>^</sup>	N	N	
300*	88,3	182,6	0,25	1,15	258	2518	482	309,6	143,5	1,0	1,0	3805	728	446,3 <sup>^</sup>	142,3 <sup>^</sup>	N	N	
320*	97,6	229,3	0,25	1,14	257	2783	532	364,4	158,8	1,0	1,0	4205	803	550,4	240,0	N	1,0	
340*	105	276,9	0,26	1,15	245	2987	581	414,2	169,2	1,0	1,0	4513	877	625,6	255,6	4,0	1,0	
360*	112	330,9	0,26	1,15	235	3195	633	467,4	179,6	1,0	1,0	4827	956	706,1	271,2	1,0	1,0	
400*	125	450,7	0,28	1,16	211	3558	741	573,4	195,4	1,0	1,0	5375	1119	866,1	295,1	0,20	1,0	
450	140	637,2	0,29	1,17	202	3984	850	719,7	216,1	1,0	1,0	6019	1284	1087	326,4	0,18	1,0	
500	155	869,7	0,30	1,18	194	4421	965	883,8	236,9	1,0	1,0	6679	1458	1335	357,9	0,16	0,22	
550	166	1119	0,32	1,19	178	4739	1082	1034	247,7	0,23	1,0	7159	1634	1563	374,2	0,15	0,20	
600	178	1412	0,34	1,20	165	5068	1204	1198	258,6	0,22	1,0	7656	1819	1809	390,7	0,13	0,19	
650	190	1752	0,35	1,22	153	5408	1333	1373	269,6	0,21	0,28	8170	2014	2075	407,3	0,12	0,18	
700	204	2153	0,38	1,23	138	5830	1511	1574	281,3	0,22	0,29	8807	2283	2377	424,9	0,13	0,19	
800	224	3034	0,41	1,26	132	6397	1794	1947	293,7	0,18	0,25	9664	2710	2941	443,7	0,09	0,15	
900	252	4221	0,44	1,28	120	7174	2110	2420	316,6	0,16	0,24	10840	3188	3655	478,2	0,07	0,13	
1000	272	6538	0,46	1,30	108	7763	2385	2870	328,9	0,13	0,20	11730	3603	4336	496,9	0,04	0,10	

Verfahren/éthode EE





Raster: Einfluss Eigenlast quer berücksichtigen.

Shaded area: Consider the effect of dead weight.

Knicklänge in [m] - Buckling length in [m]													HEA
4.5	5.0	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	10.0	12.0	15.0	
232	230	173	150	131	116	102	91	82	74	61			100
345	07	271	240	212	189	168	151	136	123	102	73		120
493	451	410	370	333	300	270	244	221	201	188	121		140
666	624	579	534	489	447	408	372	340	311	282	191	128	160
826	786	743	698	651	606	560	517	477	440	375	278	187	180
1021	981	939	893	845	796	746	697			522	394	269	200
1258	1218	1176	1130	1082	1031	978	925	871	818	719	553	384	220
1539	1499	1456	1410	1361	1309	1255	1199	1141	1082	968	763	540	240
1771	1731	1689	1645	1597	1547	1494	1438	1380	1320	1189	970	700	260
2014	1975	1933	1889	1843	1794	1742	1687	1630	1570	1447	1200	886	280
2354	2312	2269	2223	2175	2124	2071	2014	1955	1893	1764	1493	1128	300
2630	2588	2544	2498	2451	2401	2348	2293	2235	2175	2046	1770	1370	320
2844	2802	2759	2714	2667	2618	2567	2514	2457	2399	2274	2000	1	340
3063	3021	2978	2934	2888	2839	2789	2737	2683	2625	2504	2234	1806	360
3491	3464	3437	3409	3379	3348	3316	3281	3245	3206	3120	2909	2490	400
3937	3911	3885	3858	3830	3802	3772	3740	3708	3673	3599	3421	3063	450
4393	4368	4342	4316	4290	4262	4234	4205	4175	4143	4076	3920	3613	500
4732	4707	4683	4658	4633	4607	4580	4553	4525	4495	4434	4295	4031	550
5069	5055	5031	5007	4982	4957	4932	4906	4879	4852	4795	4668	4434	600
5407	5407	5386	5362	5339	5314	5289	5264	5239	5212	5158	5039	4825	650
5830	5830	5826	5802	5778	5754	5730	5705	5679	5654	5600	5486	5285	700
6396	6396	6396	6396	6379	6356	6333	6309	6286	6261	6212	6108	5932	800

Knicklänge in [m] - Buckling length in [m]													HEA
4.5	5.0	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	10.0	12.0	15.0	
259	218	185	159	138	121	106	95	84	76	62			100
407	350	302	262	229	201	178	159	142	128	105	75		120
615	642	476	419	369	327	291	261	234	212	175	125		140
870	787	706	631	563	504	452	407	367	333	277	199	131	160
1118	1034	947	863	782	708	641	581	528	481	403	292	194	180
1414	1329	1238	1146	1055	967	884	808	739	677	571	418	280	200
1772	1687	1595	1498	1399	1299	1202	1110	1024	944	805	597	403	220
2195	2109	2016	1917	1813	1705	1597	1490	1388	1290	1114	838	572	240
2548	2464	2374	2277	2174	2066	1955	1842	1731	1622	1420	1086	751	260
2916	2834	2748	2651	2550	2444	2332	2218	2101	1985	1761	1373	962	280
3423	3337	3246	3148	3045	2935	2819	2698	2574	2448	2198	1715	1240	300
3839	3754	3663	3568	3466	3358	3244	3124	3000	2872	2612	2117	1530	320
4164	4080	3991	3898	3799	3694	3584	3467	3346	3220	2959	2441	1795	340
4495	4412	4325	4233	4137	4035	3927	3814	3695	3572	3313	2781	2081	360
5190	5137	5081	5021	4958	4890	4816	4736	4649	4554	4341	3820	2958	400
5866	5816	5764	5709	5652	5591	5526	5456	5382	5302	5123	4679	3843	450
6557	6509	6459	6407	6353	6297	6237	6175	6108	6038	5883	5503	4745	500
7072	7025	6978	6929	6878	6826	6771	6714	6654	6591	6455	6127	5469	550
7598	7553	7507	7460	7412	7362	7311	7258	7203	7145	7021	6711	6157	600
8134	8090	8046	8000	7953	7906	7856	7806	7753	7699	7584	7319	6807	650
8799	8755	8710	8665	8619	8572	8523	8474	8423	8371	8260	8011	7541	700
9663	9661	9619	9576	9532	9488	9443	9397	9350	9302	9203	8985	8592	800
10836	10836	10836	10797	10754	10710	10666	10621	10576	10529	10434	10229	9873	900
11725	11725	11725	11725	11693	11650	11607	11564	11521	11476	11386	11194	10871	1000

Bemessungswerte  
 Treppenlinie für  
 kg = 50 - 100 - 200, maJ- K - 250  
 Raster: Einfluss Eigenlast quer berücksichtigen.

Calculation values  
 Broken lines for  
 OK= 50 - 100 - 200, max. OK= 250  
 Shaded area: Consider the effect of dead weight.

S235	HEA	m kg/m	A mm <sup>2</sup>	ip m	Knicklänge in [m] - Buckling length in [m]									
					0.0	1.0	2.0	2.2	2.4	2.6	2.8	3.0	3.2	3.4
					100	16.7	2120	25.1	474	420	300	275	251	229
120	19.9	2530	30.2	566	522	409	384	35s	32s		310	272	236	
140	24.7	3140	35.2	703	666	550	524	498	471	445	418	393	368	
160	30.4	3880	39.8	868	839	715	688	660	632	603	574	544	516	
180	35.5	4530	45.2	1014	996	871	844	817	789	760	730	701	671	
200	42.3	5380	49.8	1204	1196	1063	1035	1006	977	947	916	884	852	
220	50.5	6430	55.1	1439	1439	1302	1272	1242	1211	1180	1147	1114	1081	
240	60.3	7680	60.0	1719	1719	1583	1551	1519	1486	1452	1418	1382	1347	
260	68.2	8680	65.0	1943	1943	1816	1784	1750	1716	1682	1647	1611	1575	
280	76.4	9720	70.0	2178	2178	2062	2028	1994	1959	1924	1888	1852	1815	
300	88.3	11250	74.9	2518	2518	2410	2373	2337	2299	2262	2224	2185	2146	
320	97.6	12440	74.9	2784	2784	2665	2624	2584	2543	2501	2459	2416	2373	
340	105	13350	74.6	2988	2988	2858	2815	2771	2726	2682	2636	2590	2543	
360	112	14280	74.3	3196	3196	3055	3009	2961	2914	2866	2817	2767	2717	
400	125	15900	73.4	3559	3559	3444	3406	3367	3327	3287	3245	3202	3157	
450	140	17800	72.9	3984	3984	3852	3809	3766	3721	3675	3628	3579	3528	
500	155	19750	72.4	4420	4420	4271	4223	4174	4124	4073	4020	3965	3908	
550	166	21180	71.5	4740	4740	4574	4522	4468	4414	4358	4300	4240	4178	
600	178	22650	70.5	5069	5069	4883	4827	4769	4709	4648	4585	4519	4452	
650	190	24160	69.7	5407	5407	5202	5141	5078	5013	4947	4879	4808	4734	
700	204	26050	68.4	5820	5830	5597	5529	5459	5388	5315	5239	5160	5078	
800	224	28580	66.5	6396	6396	6119	6042	5963	5882	5798	5711	5620	5527	
900	252	32050	65.0	7173	7173	6842	6753	6662	6568	6471	6370	6264	6155	
1000	272	34680	63.5	7762	7762	7381	7282	7180	7075	6966	6852	6734	6611	

S355	HEA	kg/m	A mm <sup>2</sup>	ip mm	Knicklänge in [m] - Buckling length in [m]									
					0.0	1.0	2.0	2.2	2.4	2.6	2.8	3.0	3.2	3.4
					100	16.7	2120	25.1	717	596	369	330	294	262
120	19.9	2530	30.2	855	752	531	485	442	402	366	333	0	27	
140	24.7	3140	35.2	1062	968	741	691	642	594	548	505	466	429	
160	30.4	3880	39.8	1312	1226	985	932	878	823	770	719	669	623	
180	35.5	4530	45.2	1532	1462	1222	1169	1115	1059	1004	948	894	841	
200	42.3	5380	49.8	1819	1761	1507	1452	1395	1337	1278	1218	1158	1098	
220	50.5	6430	55.1	2174	2132	1863	1805	1746	1685	1622	1558	1494	1429	
240	60.3	7680	60.0	2597	2573	2280	2218	2155	2089	2023	1954	1885	1814	
260	68.2	8680	65.0	2935	2933	2629	2566	2501	2435	2367	2298	2227	2155	
280	76.4	9730	70.0	3290	3290	2997	2932	2866	2799	2730	2659	2587	2513	
300	88.3	11250	74.9	3804	3804	3514	3444	3374	3302	3229	3155	3078	3001	
320	97.6	12440	74.9	4206	4206	3885	3809	3731	3652	3571	3488	3404	3318	
340	105	13350	74.6	4514	4514	4166	4084	4000	3914	3827	3738	3647	3554	
360	112	14280	74.3	4828	4828	4453	4364	4274	4182	4088	3993	3895	3795	
400	125	15900	73.4	5376	5376	5069	4995	4918	4838	4755	4668	4578	4483	
450	140	17800	72.9	6018	6018	5669	5585	5498	5408	5314	5216	5113	5006	
500	155	19750	72.4	6677	6677	6284	6190	6093	5991	5886	5776	5661	5540	
550	166	21180	71.5	7161	7161	6726	6624	6518	6407	6292	6171	6045	5913	
600	178	22650	70.5	7658	7658	7178	7066	6950	6829	6703	6571	6433	6288	
650	190	24160	69.7	8168	8168	7643	7522	7396	7265	7128	6984	6834	6676	
700	204	26050	68.4	8807	8807	8216	8082	7943	7797	7645	7485	7318	7142	
800	224	28580	66.5	9663	9663	8973	8820	8660	8494	8318	8135	7941	7738	
900	252	32050	65.0	10836	10831	10023	9846	9661	9467	9263	9048	8823	8586	
1000	272	34680	63.5	11725	11700	10801	10603	10395	10177	9948	9706	9451	9184	

Bemessungswerte  
 Treppenlinie für  
 K - 50 - 100 - 200, male K - 250  
 Raster: Einfluss Eigenlast quer berücksichtigen.

Calculation values  
 Broken lines for  
 K - 50 - 100 - 200, maJ- K ° 250  
 Shaded area: Consider the effect of clean paid.

S235	HEA	Knicklänge in [m] - Buckling length in [m]													
		3.6	3.8	4.0	4.5	5.0	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	
		100	145	133	123	101	84	71	61	52	44	38	32	27	23
120	228	211	196	163	137	117	101	88	77	68	60	52	45	38	
140	344	322	301	256	218	188	163	142	125	111	99	88	78	68	
160	488	461	434	375	324	281	246	216	191	169	151	136	123	110	
180	641	611	582	513	451	396	349	309	275	245	220	198	180	162	
200	820	788	756	677	603	538	477	425	380	341	307	278	252	227	
220	1047	1012	977	890	806	720	653	587	529	477	432	392	357	322	
240	1310	1273	1235	1140	1044	962	886	815	752	696	646	598	556	514	
260	1538	1500	1461	1363	1263	1164	1088	1014	954	904	854	804	754	704	
280	1777	1738	1699	1599	1496	1392	1289	1180	1096	1008	927	853	786	720	
300	2106	2065	2024	1918	1808	1696	1584	1473	1367	1265	1170	1082	1001	920	
320	2329	2284	2238	2120	1999	1875	1751	1629	1511	1399	1294	1197	1107	1026	
340	2495	2447	2398	2271	2140	2006	1873	1741	1615	1494	1382	1277	1181	1090	
360	2666	2613	2560	2424	2283	2140	1996	1856	1720	1591	1470	1359	1256	1165	
400	3111	3063	3014	2881	2737	2583	2420	2254	2090	1930	1776	1639	1509	1380	
450	3476	3422	3366	3216	3053	2878	2694	2507	2322	2143	1974	1817	1672	1537	
500	385 j	3789	3726	3557	3374	3178	2972	2763	2557	2358	2170	1997	1837	1692	
550	4114	4047	3978	3794	3593	3378	3154	2927	2703	2489	2289	2103	1934	1780	
600	4381	4309	4233	4030	3810	3575	3331	3085	2845	2615	2401	2204	2024	1855	
650	4658	4578	4496	4276	4036	3781	3517	3252	2994	2749	2521	2312	2122	1943	
700	4993	4905	4813	4567	4301	4018	3727	3437	3156	2892	2648	2424	2223	2034	
800	5429	5327	5221	4938	4632	4309	3979	3655	3345	3055	2790	2550	2334	2135	
900	6041	5922	5798	5468	5112	4738	4361	3985	3618	3271	2954	2666	2400	2155	
1000	6483	6349	6209	5837	5437	5021	4604	4201	3823	3474	3156	2868	2600	2355	

S355	HEA	Knicklänge in [m] - Buckling length in [m]													
		3.6	3.8	4.0	4.5	5.0	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	
		100	157	143	131	106	88	74	63	54	46	40	34	29	24
120	253	232	214	175	146	123	106	91	80	70	62	54	47	40	
140	385	366	338	281	236	200	172	149	131	115	103	92	82	72	
160	579	539	502	421	367	306	263	229	201	178	159	142	128	114	
180	790	741	696	594	509	439	381	333	294	260	232	209	188	167	
200	1040	984	929	804	697	606	529	465	411	366	327	294	266	238	
220	1364	1301	1238	1089	956	839	739	654	581	519	465	420	380	340	
240	1743	1672	1602	1430	1270	1127	1000	890	795	712	641	579	526	474	
260	2081	2007	1933	1749	1573	1410	1262	1130	1015	914	825	748	681	620	
280	2439	2363	2286	2093	1903	1723	1555	1403	1267	1146	1039	945	862	780	
300	2921	2841	2759	2551	2343	2141	1949	1771	1608	1462	1331	1215	1111	1010	
320	3230	3141	3051	2821	2591	2367	2155	1958	1779	1617	1472	1343	1229	1126	
340	3460	3364	3266	3019	2771	2530	2302	2091	1898	1725	1570	1433	1310</		

# Nomograms

Graphical method for determining the fire resistance of steel structures to EN 1993-1-2:2005

## 1 INTRODUCTION

The fire resistance requirements for steel structures - ranging from 15 to 120 minutes - are set by national regulations. These regulations take into account the number of storeys in the building, its function, the presence of flammable materials, the number of people present and the favourable effect of any active measures (sprinklers, detection, etc.). The fire resistance of construction elements is assessed either by a standard fire test in an oven, or by calculation. This technical note describes the calculation methods for steel structures in buildings, with or without fire protection. It is based on European standard EN 1993-1-2:2005 with annex Belgian national.

## 2 CALCULATION BASIS

### 2.1 Basic principles

The moment of failure of the steel structure depends on :

- **The critical temperature  $\theta_{cr}$** : the properties of steel depend on temperature - see Figure 1. The critical temperature is the failure temperature of the steel structure. This depends on the utilisation rate  $\mu_0$  :

$$\mu_0 = E_{fi,d} / R_{fi,d,0}$$

$E_{fi,d}$  The effect of design actions in the event of fire ;

$R_{fi,d,0}$  The design resistance in the event of fire at time  $t = 0$ . For beams and tensioned elements,  $R_{fi,d,0}$  is equal to the cold resistance  $R_d$  since  $\gamma_M = \gamma_{M,fi} = 1.0$ . For continuous columns over several floors, where each floor is a separate fire compartment, the buckling length can be reduced for the calculation to a value of  $\beta_{fi} = \alpha_{LCR}$ , compared with the cold design:  $\alpha = 0.5$  for columns located at an intermediate storey;  $\alpha = 0.7$  for columns on the upper floor ; In all other cases, the buckling length remains equivalent to that of the cold design ( $\alpha = 1$ ).

- **The rate of heat-up**, which depends on three factors:
  - The temperature of the fire ;
  - The mass factor  $P$  [ $m^{-1}$ ]. This is the ratio between the surface exposed to fire ( $A$ ) and the volume of steel ( $V$ ) ;
  - The contribution to fire resistance of any protective materials. This influence is determined by the thickness  $o_p$  and the thermal characteristics:
    - thermal conductivity  $\lambda_p$  [ $W/mK$ ]
    - specific heat  $c_p$  [ $J/kgK$ ]
    - density  $\rho_p$  [ $kg/m^3$ ]

The influence on fire resistance must be determined according to ENV 13381-4 or ENV 13381-8, or according to the national standard.

### 2.2 Field of application

The calculation method is valid in the following area:

- **Static structure** :
  - Tensioned elements under tension ;
  - Isostatic and hyperstatic beams subjected to bending ;
  - Columns subjected exclusively to axial loading ;
  - Elements that are sensitive to torsional buckling or subject to a combination of axial, transverse and/or moment loads do not fall within the scope of this method. There is no risk of tipping when the compressed web of the beam is supported laterally, by a floor slab for example.

for example;

- **Steel quality**: All qualities in accordance with EN 10025 ;
- **Steel sections**: Class 1, 2 or 3, see table 1 for classification. For class 4 sections, the standard critical temperature is 350°C. The mass factor must be greater than 10  $m^{-1}$ .

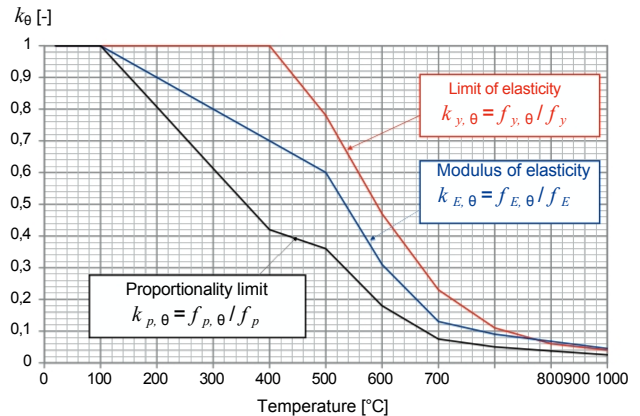


Figure 1: Reduction coefficients for the mechanical properties of steel as a function of temperature.

Table 1: Classification of sections subjected to compression.

Internal compressed walls					
Section class	Flexion	Compression			
1	$c/t \leq 72 \cdot \epsilon$	$c/t \leq 33 \cdot \epsilon$			
2	$c/t \leq 83 \cdot \epsilon$	$c/t \leq 38 \cdot \epsilon$			
3	$c/t \leq 124 \cdot \epsilon$	$c/t \leq 42 \cdot \epsilon$			
Console walls					
Section class	Flexion	Compression			
1		$c/t \leq 9 \cdot \epsilon$			
2		$c/t \leq 10 \cdot \epsilon$			
3		$c/t \leq 14 \cdot \epsilon$			
Other profiles					
Angle iron		Tubes			
Section class	Compression	Compression and/or bending			
1	-	$d/t \leq 50 \cdot \epsilon$			
2	-	$2 \cdot d/t \leq 70 \cdot \epsilon$			
3	$h/t \leq 15 \cdot \epsilon$	$\epsilon^2 \cdot d/t \leq 90 \cdot \epsilon^2$			
		For $d/t \geq 90 \cdot \epsilon^2$ , see EN 1993-1-6			
Values of $\epsilon$ and $\epsilon^2$ in the event of fire					
$f_y$	S235	S275	S355	S420	S460
$\epsilon$	0,85	0,79	0,69	0,64	0,61
$\epsilon^2$	0,72	0,62	0,48	0,40	0,37
$c$	0,12	0,02	0,70	0,70	0,01

## 2.3 Assumptions

- The evolution of the fire temperature follows the standard fire curve [ISO 834].
- Mechanical loads are constant during the fire. The effects of thermal expansion are neglected.
- The temperature in the steel structure is uniform. An uneven temperature distribution is compensated for by the correction coefficient  $\kappa = \kappa_1 \cdot \kappa_2$ .  $\kappa$  is equal to 0.6 / 0.7 / 0.85 or 1.0 with :
  - $\kappa_1$ : to take account of a temperature distribution that is not uniform in the cross-section of the beam :
    - $\kappa_1 = 0.70$ : unprotected beam, heated on three sides ;
    - $\kappa_1 = 0.85$ : protected beam, heated on three sides ;
    - $\kappa_1 = 1.00$ : beam heated on all sides ;
  - $\kappa_2$ : to take account of a temperature distribution that is not uniform along the length of the beam :
    - $\kappa_2 = 0.85$ : at the support of a hyperstatic beam ;
    - $\kappa_2 = 1.00$ : in all other cases.

## 3 ACTIONS IN THE EVENT OF EXPOSURE TO FIRE

According to Eurocode 1, including the national annex, in the event of fire, the variable vertical load  $Q_{k,i}$  must be reduced to a value that is almost equal to that of the load on the structure.

from the extreme value of the cold design by means of the reduction coefficient  $\psi_{2,i}$ . In addition, the safety coefficients applied to the loads must be equal to 1.

$$E_{fi,d} = \sum G_{k,j} + \sum \psi_{2,i} Q_{k,i}$$

The variable costs  $Q_{k,i}$ , as well as the values of  $\psi_{2,i}$  representing the quasi-permanent part of these costs, are shown in Table 2 by

depending on the purpose of the building. Depending on the ratio between  $Q_{k,i}$  and the permanent loads  $G_{k,j}$ , and depending on the number of storeys  $n$  supported by the column, the total load in the event of fire will be reduced compared to the cold design - see table 2. The load reduction coefficient can be used as a safety factor for the utilisation rate, provided that the cold design is correct. In Table 2, it is assumed that no reduction in live loads has been applied to the cold design of beams supporting large areas.

**Table 2: Vertical loads and associated reduction coefficients**

Purpose of the building and $G_k$	$Q_k$ kN/m <sup>2</sup>	$Q_k/G_k$ 2 <i>i</i>	beams columns ( $n < 2$ )		columns ( $n > 2$ )			
			0,5	1	0,5	1	2	
A: Accommodation	2,0	0,3	0,55	0,46	0,37	0,61	0,53	0,45
B: Office	3,0	0,3	0,55	0,46	0,37	0,61	0,53	0,45
C: Meeting space	5,0	0,6	0,62	0,56	0,51	0,69	0,65	0,62
D: Trade	5,0	0,6	0,62	0,56	0,51	0,69	0,65	0,62
E: Storage	7,5	0,8	0,67	0,63	0,60	0,67	0,63	0,60
F: Parking: cars < 3 T	2,5	0,6	0,62	0,56	0,51	0,69	0,65	0,62
G: Car park: cars 3-16 T	5,0	0,3	0,55	0,46	0,37	0,61	0,53	0,45
H: Roofs*)		0,0	0,48	0,35	0,23	0,57	0,46	0,33

\*) Snow load (EN 1991-1-3) and maintenance load.

## 4 CALCULATION METHOD

### 4.1 Calculating the critical temperature

The simple method can be used for beams and tensioned elements. It can also be applied to columns, but the results will be strongly on the side of safety. Dimensioning will be obtained using the method described in point 4.1.2.

#### 4.1.1 Simple method

**Step 1a:** Determine the rate of use in the event of fire

$$\mu_{0} = E f_{i,d} / R f_{i,d,0}$$

According to the Eurocode, we can consider values located on the side of the  $\mu_0 = 0.70$  for category E floors in EN 1990 (warehouses) or  $\mu_0 = 0.65$  in all other cases. For elements subject to compression, the utilisation rate can be calculated by approximation based on the strength of the cold design :

$$\mu_{0} = E f_{i,d} / R d$$

**Step 2a:** For beams, determine the correction coefficient  $\kappa$  in

as a function of the uniformity of the temperature distribution. For columns, calculate the reduction coefficient for the length of buckling in the event of fire  $\alpha$  of the storey under consideration and of the connections between the columns on the different floors.

**Step 3a:** Graphically determine the critical temperature from the

### 4.1.2 Advanced method for compression elements

**Step 1b:** More precise values can be obtained by calculating the permissible reduction coefficient of the plastic stress :

$$\mu_{pl} = E_{fi,d} / (A_a \cdot f_y)$$

Where  $A_a$  is the cross-sectional area and  $f_y$  is the cold yield strength. **Step 2b:** Calculate the slenderness at time  $t = 0$ , taking into account the reduction in buckling length:

$$\lambda_{fi,0} = \alpha \cdot \lambda = \alpha \cdot \frac{L_{cr}}{i} \quad \text{where } \varepsilon = \sqrt{235 / f_y}$$

**Step 3b:** Find the critical temperature in Table 4 from the values of  $\mu_{pl}$  and  $\lambda_{fi,0}$ .

## 4.2 Calculation of steel temperature

**Step 4:** Calculate the mass factor. This is

$$P = A / V$$

In the case of an unprotected profile or a profile with rectangular protection, the rectangular perimeter of the profile is taken as the value of the surface exposed to fire  $A$  - see table 3. For a profile with protection following the contour of the profile, the surface area of the protection is taken as the value for  $A$ . The solidity factors for exposure from all sides or from 3 sides are given in Table 6. **Step 5:** Correct the solidity factor. The values in Table 6 must be multiplied by a coefficient of 0.9 in the case of an unprotected I-section.

For protected profiles, heating is calculated using a modified mass factor as follows:

$$P_{mod} = \frac{A \cdot \lambda_p}{V d_p} \cdot \frac{1}{1 + \phi} \quad \text{where } \phi = \frac{\rho_p \cdot c_p \cdot d_p \cdot A}{\rho_a \cdot c_a \cdot V}$$

$\phi$  represents the relative thermal inertia of the insulating material,  $\rho_a$  the density of the steel (equal to 7850 kg/m<sup>3</sup>), and  $c_a$  the specific heat of steel. For calculation purposes,  $c_a$  can be approximated by 600 J/kgK. To be on the safe side,  $\phi$  can also be neglected ( $\phi = 0$ ).

**Step 6:** Using Figure 2, graphically determine the time for which the critical temperature is reached, depending on the corrected mass factor. This time is the fire resistance value.

**Table 3: Mass factors as a function of the type of profile and the heating method.**

Unprotected I-beam heated from all sides	I-beam protected and heated from all sides: rectangular protection	I-beam protected and heated from all sides: protection along the contour of the profile
$P = 0.9 \cdot A/V = 0.9 \cdot (2 \cdot b + 2 \cdot h) / V$	$P = A/V = (2 \cdot b + 2 \cdot h) / V$	$P = A/V$
Unprotected I-beam heated on 3 sides	I-beam protected and heated on 3 sides: protection rectangular	I-beam protected and heated on 3 sides: protection along the contour of the profile
$P = 0.9 \cdot A/V = 0.9 \cdot (b + 2 \cdot h) / V$	$P = A/V = (b + 2 \cdot h) / V$	$P = (A-b) / V$
Unprotected and heated L-profile from all sides	Hollow tube no protected and heated from all parts	Solid, unprotected profile heated from all sides

figure 2.

$$P = A/V \approx 2/t$$

$$P = A/V \approx 1/t$$

$$P = A/V = 4/d$$

- 2 -

$f_{y,i}$	0,0	0,2	0,4	0,6	0,8	1	1,2	1,4	1,6	1,8	2		
0	950	820	767	725	692	671	650	629	608	590	574	558	542
0,2	918	796	745	697	673	649	625	601	582	564	546	528	509
0,4	892	777	714	678	650	622	595	574	553	532	512	485	452
0,6	867	747	685	651	617	588	564	539	515	483	441	391	164
0,8	829	699	657	615	581	552	522	486	430	320	117		
1	784	674	621	578	542	506	437	316	124				
1,2	738	645	585	541	492	385	197						
1,4	694	611	552	495	346	127							
1,6	674	582	516	364	116								
1,8	652	554	436	169									
2	628	524	294										
													<b>S235</b>
0	950	820	767	725	692	671	650	629	608	590	574	558	542
0,2	921	797	747	698	675	651	627	603	584	566	548	530	512
0,4	894	780	718	680	653	625	598	578	557	536	516	493	460
0,6	871	752	688	655	622	592	568	544	520	494	453	411	246
0,8	835	703	660	619	585	557	528	499	444	367	186		
1	788	677	625	582	547	512	452	353	177				
1,2	743	648	589	545	502	407	234						
1,4	695	614	556	503	370	162							
1,6	676	585	520	384	147								
1,8	654	557	447	195									
2	630	527	312										
													<b>S275</b>
0	950	820	767	725	692	671	650	629	608	590	574	558	542
0,2	924	798	749	700	677	653	630	606	587	569	551	533	515
0,4	897	783	724	684	657	630	603	582	562	542	522	502	472
0,6	878	758	692	660	628	598	575	552	529	506	470	431	356
0,8	845	713	666	627	591	564	537	509	466	413	278		
1	795	681	632	588	555	521	474	403	250				
1,2	752	653	594	552	511	430	288	101					
1,4	698	620	562	511	403	213							
1,6	679	589	526	409	191								
1,8	658	562	465	230									
2	634	532	337										
													<b>S355</b>
0	950	820	767	725	692	671	650	629	608	590	574	558	542
0,2	926	799	750	702	678	654	631	608	588	571	553	535	517
0,4	899	786	727	686	660	633	607	585	566	546	526	506	479
0,6	881	762	694	663	632	602	579	556	534	511	481	442	404
0,8	851	719	669	631	595	569	542	515	479	428	329	144	
1	800	683	636	592	559	527	488	419	292	117			
1,2	757	656	597	556	516	444	318	143					
1,4	700	623	565	515	416	241	292	111					
1,6	681	591	530	422	216	217							
1,8	660	564	475	250	194								
2	636	535	351	395	171								
													<b>S420</b>
0	950	820	767	725	692	671	650	629	608	590	574	558	542
0,2	927	799	751	703	678	655	632	609	589	571	554	536	518
0,4	900	787	729	687	661	635	609	587	567	548	528	509	483
0,6	883	764	695	665	635	604	581	559	536	514	486	448	411
0,8	853	722	670	633	597	571	545	519	485	435	354	181	
1	803	685	638	594	562	530	495	426	312	145			
1,2	759	657	598	558	519	451	332	164					
1,4	702	625	567	518	423	255							
1,6	682	592	532	428	228								
1,8	661	566	481	260									
2	637	536	358	241									
													<b>S460</b>

## 5 INSULATION PROPERTIES

Indicative values of the thermal characteristics of different insulating materials - see Table 5 - can be used for an initial calculation of the heating of the steel. For a definitive determination of the thickness required, refer to the certificates issued by the suppliers of insulating materials.

Table 5: Indicative values for the thermal characteristics of different insulation materials.

Insulating material	$\rho_p$ [kg/m <sup>3</sup> ]	$\lambda_p$ [W/mK]	$C_p$ [J/kgK]
Sprayed insulation, low density :			
- mineral fibres	300	0,12	1200
- vermiculite cement or perlite	350	0,12	1200
Sprayed insulation, high density :			
- vermiculite or perlite with cement	550	0,12	1100
- vermiculite or perlite with plaster	650	0,12	1100
Board insulation :			
- vermiculite or perlite with cement	800	0,20	1200
- silicate (calcium) fibres	600	0,15	1200
- fibre cement	800	0,15	1200
- plaster	800	0,20	1700
Mineral wool	150	0,20	1200
Intumescent paint	0	0,005 - 0,012	0

## 6 SYMBOLS

- $\alpha$  Buckling length reduction coefficient for columns in the event of fire [-]
- $\varepsilon$  Dimensionless quantity for local and global instability [-]
- $\Phi$  Relative thermal inertia of insulating material [-]
- $\gamma_M$  Partial coefficient of material in cold = 1 [-]
- $\gamma_{M,fi}$  Partial coefficient of material in fire = 1 [-]
- $K$  Product of temperature gradient correction coefficients [-]
- $\kappa_1$  Temperature gradient correction coefficient in section [-]
- $\kappa_2$  Temperature gradient correction coefficient along length [-]
- $\lambda$  Relative elongation in cold [-]
- $\lambda_{fi,t}$  Relative expansion in the event of fire at time  $t = 0$  [-]
- $\lambda_p$  Thermal conductivity of the insulating material [W/mK]
- $\mu$  Utilisation rate [-]
- $\mu_{pl}$  Plastic utilisation rate [-]
- $\rho_a$  Steel density = 7850 [kg/m<sup>3</sup>]
- $\rho_p$  Density of insulating material [kg/m<sup>3</sup>]
- $\theta_{cr}$  Critical temperature [°C]
- $\psi_{2,i}$  Reduction coefficient of quasi-permanent load  $i$  [-]
- $A$  Area of steel section exposed to fire [m<sup>2</sup>]
- $J$  Cross-sectional area of steel section [m<sup>2</sup>]
- $J_{E,fi,d}$  Effect of design actions in the event of fire
- $Gk_i$  Characteristic value of permanent loads  $i$
- $L_{cr}$  Cold buckling length [m]
- $M_{fi,Ed}$  Design value of bending moment in the event of fire [kNm]
- $M_{fi,Rd}$  Design value of resisting moment in the event of fire [kNm]
- $P$  Mass factor [m<sup>-1</sup>]
- $P_{mod}$  Modified mass factor for a protected profile [W/m<sup>3</sup> K]
- $Qk_i$  Characteristic value of variable loads  $i$
- $R_d$  Calculation value for cold resistance
- $R_{fi,d,t}$  Design value of resistance in the event of fire at time  $t = 0$
- $V$  Volume of steel section [m<sup>3</sup>]
- $b$  Profile width [m]
- $c$  Core length for section classification [m]
- $c_a$  Specific heat of steel  $\approx$  600 [J/kgK]
- $c_p$  Specific heat of the insulating material [J/kgK]
- $d$  Tube diameter [mm]
- $\delta_p$  Dry thickness of insulation material [m]
- $f_y$  Yield strength of cold rolled steel [N/mm<sup>2</sup>]
- $h$  Profile height [m]
- $i$  Radius of inertia of profile along weak or strong axis [m]
- $k_{E,\theta}$  Coefficient of reduction in modulus of elasticity in the case of fire [-]
- $k_{p,\theta}$  Coefficient of reduction of the proportionality limit in the event of fire [-]
- $k_{y,\theta}$  Coefficient of reduction in yield strength for fire [-]
- $l_{fi}$  Buckling length in the event of fire [m]
- $n$  Number of floors supported by the column
- $q_{fi,Ed}$  Uniformly distributed linear load in the event of fire [kN/m]
- $t$  Time elapsed since start of fire [min]
- $t$  Wall thickness for section classification [m]

## 7 REFERENCES

- EN 10025-1: 2005, *Hot rolled products of structural steels - Part 1: General technical delivery conditions*, CEN, Brussels, Belgium
- EN 1990: 2005, *Eurocode 0: Basis of design*, CEN, Brussels, Belgium.
- EN 1991-1-2: 2002, *Eurocode 1: Actions on structures - Part 1-2: General actions - Actions on structures exposed to fire*, CEN, Brussels, Belgium.
- EN 1991-1-3: 2003, *Eurocode 1: Actions on structures - Part 1-3: General actions - Snow loads*, CEN, Brussels, Belgium.
- EN 1993-1-1: 2005, *Eurocode 3: Design of steel structures - Part 1-1: General rules and rules for buildings*, CEN, Brussels, Belgium.
- EN 1993-1-2: 2005, *Eurocode 3: Design of steel structures - Part 1-2: General rules - Structural fire design*, CEN, Brussels, Belgium.
- ISO 834: 1999, *Fire resistance tests - Elements of building construction - Part 1: General requirements*, ISO, Geneva, Switzerland.

## 8 CONTACT

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[helpdesk@infosteel.be](mailto:helpdesk@infosteel.be)  
[www.infosteel.be](http://www.infosteel.be)





## 9 CALCULATION EXAMPLES

### 9.1 Isostatic beam

**Data :** S235 steel IPE300 beam supporting a composite floor in an office building. The plastic moment at normal temperature is  $M_{fi,0,Rd} = 147.7$  kNm. The beam is protected by intumescent paint with a dry thickness of 1 mm. Span 6 m. The centre-to-centre distance of the beams is 3 m. The dead weight of the floor, including finishes, is  $G_k = 3$  kN/m<sup>2</sup>. The dead weight of the beam is 0.4 kN/m'. The live load for an office building in Belgium is  $Q_k = 3$  kN/m<sup>2</sup>.

**Unknown:** Determine fire resistance.

#### 9.1.1 Simple calculation

**Step 1:** Determine the utilisation rate. The simplest approximation is the approach from the safety side:  $\mu_0 = 0.65$ .

**Step 2:** Determine the correction coefficient. The upper core is

not subject to the tilting moment, since it is retained by the slab: the  $\kappa$  coefficients are therefore applicable. For an isostatic beam protected with a concrete slab on the upper face :

$$\kappa = 0.85.$$

**Step 3:** Determine the critical temperature from Figure 2.

$$\theta_{cr} = 573 \text{ }^\circ\text{C}.$$

**Step 4:** Determine the mass factor from Table 6. For protection following the contour of the profile, we obtain  $P = 188 \text{ m}^{-1}$ .

**Step 5:** Correct the mass factor, with  $\lambda_p = 0.01 \text{ W/mK}$ .

The thermal inertia of the intumescent paint is negligible ( $\phi = 0$ ).

$$P_{mod} = \frac{A \cdot \lambda_p \cdot 1}{V d_p (1 + \phi)} = 188 \cdot \frac{0.01}{0.001 \cdot 1 + 0} = 1880 \text{ W/m}^3 \text{ K}$$

**Step 6:** Graphically determine the fire resistance according to the figure 2:  $t = 50$  min. The beam complies with R30.

#### 9.1.2 Precise calculation

**Step 1:** Determine the utilisation rate :

The load in the event of fire is equal to :

$$q_{fi,Ed} = 1.0 \cdot (3 \cdot 3 + 0.4) + 1.0 \cdot 0.3 \cdot 3 \cdot 3 = 12.1 \text{ kN/m}$$

$$M_{fi,Ed} = \frac{1}{8} \cdot 12.1 \cdot 6^2 = 54.5 \text{ kNm}$$

$$\mu_0 = \frac{54.5}{147.7} = 0.37$$

**Step 2:** See 9.1.1:  $\kappa = 0.85$ .

**Step 3:** See Figure 2:  $\theta_{cr} = 665^\circ\text{C}$ .

**Steps 4 and 5:** See 9.1.1:  $P_{mod} = 1880 \text{ W/m}^3 \text{ K}$ .

**Step 6:** The fire resistance is 66 minutes, so the beam complies with R60.

### 9.2 Hyperstatic beam

**Data:** Same beam as in 9.1, but hyperstatic.

**Unknown:** Determine the thickness of the insulation (silicate boards, etc.) limestone) required for 120 minutes fire resistance.

**Step 1:** By approximation, the bending moment is :

$$M_{fi,Ed} = \frac{1}{12} \cdot 12.1 \cdot 6^2 = 36.3 \text{ kNm}$$

This gives  $\mu_0 = 36.3 / 147.7 = 0.25$ .

**Step 2:** This is a hyperstatic beam protected and heated from three sides, so  $\kappa = 0.85 - 0.85 = 0.7$ .

**Step 3:** See Figure 2:  $\theta_{cr} = 748^\circ\text{C}$ .

**Step 4:** For rectangular insulating protection, Table 6 gives us gives  $P = 139 \text{ m}^{-1}$ .

To satisfy R120, we can see from Figure 2 that a modified mass factor  $P_{mod} = 1350 \text{ W/m}^3 \text{ K}$  is required. As a first approximation, we neglect the thermal inertia of the insulation ( $\phi = 0$ ).

With  $\lambda_p = 0.15 \text{ W/mK}$ , a thickness of :

$$d_p = \frac{A \cdot \lambda_p \cdot 1}{V_{P_{mod}} (1 + \phi)} = 139 \cdot \frac{0.15 \cdot 1}{1350 (1 + 0)} = 15.4 \text{ mm}$$

Let's calculate the difference in thickness, taking into account the thermal inertia of the insulation. Using  $d_p = 15.4 \text{ mm}$  and Table 5, we obtain :

$$\phi = \frac{\rho_a \cdot c_a \cdot d_p \cdot A}{P \cdot V} = \frac{600 \cdot 1200}{600 \cdot 7850} \cdot 0.0154 \cdot 139 = 0.33$$

This value gives a minimum thickness of :

### 9.3 Unprotected hyperstatic beam

**Data :** Beam from point 9.2 without protection, but in high-quality steel.

**Unknown:** Check that the beam complies with R30.

**Step 1:** Using S355 steel, the utilisation rate becomes :

$$\mu_0 = 235 / 355 - 0.25 = 0.16$$

**Step 2:** An unprotected, heated hyperstatic beam of three sides, so :

$$\kappa = 0.7 - 0.85 = 0.6$$

**Step 3:** See Figure 2:  $\theta_{cr} = 825^\circ\text{C}$ .

**Step 4:** We use the mass factor for protection rectangular :

$$P = 139 \text{ m}^{-1}$$

**Step 5:** The mass factor of an unprotected I-section must be modified by a coefficient of 0.9:  $P = 0.9 \cdot 139 = 125 \text{ m}^{-1}$ .

**Step 6:** The fire resistance is 32 minutes. The beam therefore complies with R30.

### 9.4 Column subjected to an axial load

**Data:** HEA 200 column in S235 steel, subjected exclusively to axial forces. The radius of inertia along the weak axis is  $i = 49.8 \text{ mm}$  and the cross-sectional area is  $A_a = 5383 \text{ mm}^2$ . The column is protected by 20 mm thick plasterboard. The height of the storey is 3 m. The load-bearing capacity for the cold design is  $R_d = 962 \text{ kN}$ . Consider a continuous column located at an intermediate storey. The column carries 5 storeys with the beam from example 9.1 on each side of the column.

**Unknown:** Determine fire resistance.

#### 9.4.1 Simple method with estimated utilisation rate

**Step 1:** Determine the utilisation rate. The  $Q_k / G_k$  ratio is equal to :

$$Q_k / G_k = (3 - 3) / (3 - 3 + 0.4) \approx 1.$$

Table 2 shows that fire loads are reduced to 0,53. This value of  $\mu_0$  is on the safe side.

**Step 2:** Determine the correction coefficient. For a column located on an intermediate storey, the buckling length can be

halved:  $\alpha = 0.5$ .

**Step 3:** Determine the critical temperature from Figure 2.

$$\theta_{cr} = 560 \text{ }^\circ\text{C}.$$

**Step 4:** Determine the mass factor. For a profile with rectangular protection, Table 6 gives  $P = 145 \text{ m}^{-1}$ .

**Step 5:** Correct the mass factor :

$$\phi = \frac{\rho_a \cdot c_a \cdot d_p \cdot A}{P \cdot V} = \frac{800 \cdot 1700}{145 \cdot 600 \cdot 7850} \cdot 0.02 \cdot 145 = 0.84$$

$$P_{mod} = \frac{A \cdot \lambda_p \cdot 1}{V d_p (1 + \phi)} = 145 \cdot \frac{0.15}{0.02 \cdot 1 + 0.84} = 1134 \text{ W/m}^3 \text{ K}$$

**Step 6:** Graphically determine the fire resistance according to the figure 2:  $t = 70$  minutes. The column satisfies R60.

#### 9.4.2 Simple method with precise calculation of the utilisation rate

**Step 1:** The column supports 5 - 2 = 10 beams, as described in section 9.1.

$$E_{fi,d} = 10 \cdot 12.1 \cdot 6 / 2 = 363 \text{ kN}$$

To apply the curves in Figure 2 ( $\alpha = 0.5 / 0.7$  and 1), the rate must be calculated:

$$\mu_0 = E_{fi,d} / R_d = 363 / 962 = 0.38$$

**Step 2:** See 9.4.1:  $\alpha = 0.5$ .

**Step 3:** See Figure 2:  $\theta_{cr} = 618^\circ\text{C}$ .

**Steps 4 and 5:** See 9.4.1:  $P_{mod} = 1134 \text{ W/m}^3 \text{ K}$ .

**Step 6:** The fire resistance is 83 minutes. The column therefore complies with R60.

#### 9.4.3 Precise method

**Step 1:** Determine the plastic utilisation rate :

$$\mu_{pl} = E_{fi,d} / (A_a \cdot f_y) = 363 / (5383 - 235) = 0.29$$

**Step 2:** Calculate the slenderness at time  $t = 0$  :

$$\lambda_{fi,0} = \alpha \cdot \lambda = \alpha \cdot \frac{L_{cr}}{i} = 0.5 \cdot \frac{3000}{49.8} = 0.32$$

**Step 3:** Determine the critical temperature from Table 4 :

$$\theta_{cr} = 639 \text{ }^\circ\text{C}.$$

**Steps 4 and 5:** see 9.4.1:  $P_{mod} = 1134 \text{ W/m}^3 \text{ K}$ .

$$d_p = 15.4 / (1 + 0.33 / 3) = 13.9 \text{ mm}$$



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**Table 6: Mass factors for steel sections. For unprotected I- and H-sections, the values given for the section with rectangular protection must be multiplied by a coefficient of 0.9.**





																				
HEAA					HEA					HEB					HEM					
100	181	288	245	353	100	137	217	185	264	100	115	180	154	219	100	65	97	85	116	
120	182	296	247	361	120	137	221	185	268	120	106	168	141	203	120	61	92	80	111	
140	172	282	233	343	140	129	207	174	251	140	98	156	130	189	140	58	89	76	107	
160	150	244	203	296	160	120	193	161	235	160	88	140	118	170	160	54	83	71	100	
180	141	230	190	279	180	115	186	155	225	180	83	132	110	159	180	52	80	68	96	
200	130	211	175	256	200	108	175	145	212	200	77	122	102	147	200	49	76	65	91	
220	122	200	165	243	220	99	162	134	196	220	72	115	97	139	220	47	73	62	88	
240	114	185	154	225	240	91	147	122	178	240	68	108	91	130	240	39	61	52	73	
260	108	175	146	213	260	88	141	117	170	260	66	105	88	127	260	39	60	51	72	
280	104	168	139	204	280	84	136	113	165	280	64	102	85	123	280	38	58	50	70	
300	97	159	131	192	300	78	126	105	153	300	60	96	80	116	300	33	50	43	60	
320	95	152	127	184	320	74	117	98	141	320	58	91	77	110	320	33	50	43	60	
340	94	147	123	177	340	72	112	94	135	340	57	88	75	106	340	34	50	43	60	
360	92	142	120	170	360	70	107	91	128	360	56	86	73	102	360	34	51	44	61	
400	90	135	115	161	400	68	101	87	120	400	56	82	71	98	400	36	52	45	61	
450	90	132	114	156	450	66	96	83	113	450	55	79	69	93	450	38	53	47	63	
500	91	130	113	152	500	65	92	80	107	500	54	77	67	89	500	39	54	48	63	
550	88	123	108	143	550	65	90	79	104	550	55	76	67	87	550	41	56	50	64	
600	88	120	106	138	600	65	89	79	102	600	56	75	67	86	600	42	57	51	65	
650	88	118	105	135	650	65	87	78	100	650	56	74	66	85	650	44	58	52	66	
700	86	114	102	129	700	64	85	76	96	700	55	72	65	82	700	45	59	53	67	
800	84	108	98	122	800	66	84	76	94	800	57	72	66	81	800	48	61	55	68	
900	81	102	93	113	900	65	81	74	90	900	57	70	65	78	900	50	62	57	69	
1000	79	98	90	108	1000	66	81	74	89	1000	58	70	65	78	1000	52	64	59	70	
CAI					IPE A					IPE O					HL					
80	270	369	330	429	80	317	429	389	502	80	168	228	202	262	1000 AA	71	93	83	105	
100	247	334	300	388	100	286	393	349	456	100	158	212	190	244	1000 A	58	76	68	86	
120	230	315	279	363	120	271	368	329	426	120	149	200	179	230	1000 B	51	66	59	74	
140	215	290	259	335	140	260	356	314	411	140	139	185	167	213	1000 M	46	60	54	67	
160	200	268	241	309	160	245	333	295	383	160	127	170	152	195	1000 x 477	40	52	47	58	
180	188	254	226	292	180	227	306	274	352	180	121	162	145	186	1000 x 554	35	45	41	51	
200	176	235	211	270	200	210	281	253	324	200	114	153	137	175	1000 x 642	31	39	36	44	
220	165	222	198	255	220	192	258	231	297	220	107	142	127	163	1000 x 748	27	34	31	38	
240	153	204	184	235	240	178	240	214	276	240	103	135	122	154	1100 A	59	76	68	85	
270	147	197	176	226	270	171	231	205	266	270	94	121	110	138	1100 B	52	67	60	75	
300	139	188	167	216	300	160	217	192	249	300	89	114	104	129	1100 M	47	61	55	68	
330	131	174	157	200	330	149	199	178	228	330	85	107	98	121	1100 R	42	53	48	59	
360	122	162	146	186	360	138	184	165	211	360	73	93	85	104						
400	116	153	137	174	400	133	175	158	200											
450	110	144	130	163	450	127	165	149	187											
500	104	133	121	151	500	118	152	138	172											
550	97	124	113	140	550	111	142	129	160											
600	91	115	105	129	600	103	131	119	147											
750 x 137	101	129	116	144																
750 x 147	94	120	109	134																
750 x 173	81	102	93	114																
750 x 196	72	91	83	102																
UPE					L					HD					HE					
80	209	291	258	341	90 x 90 x 9	143	168	201	226	260 x 54.1	108	175	146	213	400 x 299	31	45	40	53	
100	204	278	248	322	100 x 100 x 8	159	187	223	251	260 x 68.2	88	141	117	170	400 x 347	28	40	35	47	
120	195	259	233	298	100x10 0x 10	129	151	181	204	260 x 93	66	105	88	127	400 x 403	25	35	31	41	
140	187	247	223	282	100 x 100 x 12	109	128	153	172	260 x 114	55	86	73	104	400 x 468	22	31	27	36	
160	180	235	212	267	110 x 110 x 10	128	151	180	203	260 x 142	46	71	60	85	450 x 312	33	46	40	53	
180	173	225	203	254	110 x 110 x 12	108	127	152	171	260 x 172	39	60	51	72	450 x 368	28	39	35	46	
200	165	213	193	240	120 x 80 x 8	174	201	225	252	260 x 225	31	47	40	56	450 x 436	25	34	30	40	
220	155	198	180	223	120 x 80 x 10	141	163	183	204	260 x 299	25	37	32	44	450 x 519	22	29	26	34	
240	148	188	171	211	120 x 120 x 11	117	138	164	185	320 x 74.2	95	152	127	184	500 x 320	34	47	41	54	
270	142	178	163	199	120 x 120 x 12	108	127	151	170	320 x 97.6	74	117	98	141	500 x 379	29	40	36	47	
300	124	153	141	171	120 x 120 x 13	100	118	141	158	320 x 127	58	91	77	110	500 x 451	25	34	31	40	
330	113	138	128	153	120 x 120 x 15	88	103	123	138	320 x 158	48	74	63	89	500 x 534	22	30	27	35	
360	107	130	121	144	130 x 130 x 12	107	126	150	170	320 x 198	39	60	51	73	550 x 330	35	48	42	55	
400	100	120	112	133	140 x 140 x 13	99	116	139	157	320 x 245	33	50	43	60	550 x 393	30	41	37	47	
					150 x 90 x 10	143	164	182	203	320 x 300	28	42	36	50	550 x 466	26	35	32	40	
					150 x 90 x 11 cm	131	150	166	185	320 x 368	24	35	30	42	550 x 552	23	30	28	35	
					150 x 100 x 10	139	161	180	203	320 x 451	20	29	26	35	600 x 340	36	48	43	55	
					150 x 100 x 12	117	136	152	170	360 x 134	63	104	85	125	600 x 402	31	42	38	48	
					150 x 150 x 12	106	125	149	168	360 x 147	58	95	78	114	600 x 477	27	36	32	41	
					150 x 150 x 14	92	108	129	145	360 x 162	53	87	71	105	600 x 564	24	31	28	35	
					150 x 150 x 15	86	101	121	136	360 x 179	49	79	65	95	650 x 347	38	49	45	56	
					150 x 150 x 18	73	85	102	115	360 x 196	45	72	60	87	650 x 410	33	42	39	48	
					160 x 160 x 15	86	101	121	136	400 x 187	47	78	64	94	650 x 487	28	36	33	42	
					160 x 160 x 17	76	90	107	121	400 x 216	42	68	56	82	650 x 579	24	31	29	36	
					180 x 180 x 16	74	95	107	128	400 x 237	38	63	52	76	700 x 356	39	50	46	57	
					180 x 180 x 18	66	85	96	114	400 x 262	35	57	47	69	700 x 421	34	43	39	49	
					200 x 100 x 10	4347	167	181	201	400 x 287	32	52	43	63	700 x 500	29	37	34	42	
					200 x 100 x 12	177	167	148	153	400 x 314	30	48	40	58	700 x 594	25	32	29	36	
					200 x 100 x 14	187	121	132	132	400 x 347	28	44	37	53	800 x 377	41	51	47	58	
					200 x 100 x 16	80	80	95	112	400 x 382	25	40	34	49	800 x 448	35	44	40	49	
					200 x 200 x 20	44	65	77	91	400 x										



Figure 2: Nomogram for determining critical temperature and fire resistance.

